

LVRJHQLHV & LVRPHWULHV

Nulmq Uhlmqghuv - 10.30 - Pdb 12, 2025

LV R J H Q L H V & L V R P H W U L H V

G
H
I
J
K
L
M
N
O
P
Q

LV R J H Q L H V & L V R P H W U L H V

F
G
H
I
J
K
L
M
N
O
P

KV R J H Q L H V & L V R P H W U L H V

E
F
G
H
I
J
K
L
M
N
O

J V R J H Q L H V & L V R P H W U L H V

E

F

G

H

IVRJHQLHV & LVRPHWULHV

J

K

L

M

N

QMECLGCU & GQMKCRPJCU
ERNFDMHDR & HRNLD SQHDR
FSOGENIES & ISOMETRIES
GTPHF0JFT & JTPNFUSJFT
HUQIGPKGU & KUQOGVTKGU
IVRJHQLHV & **L**VRPHWULHV

J
K
L
M
N

P	L	D	B	R	F	B	P	
E	Q	M	E	C	L	G	C	Q
F	R	N	F	D	M	H	D	R
G	S	O	G	E	N	I	E	S
H	T	P	H	F	O	J	F	T
I	U	Q	I	G	P	K	G	U
J	V	R	J	H	Q	L	H	V
K								
L								
M								
N								

EPLDBKFBP & FPLJBQOFBP

FQMECLGCQ & GQMKCRPGCQ

GRNFDMHDR & HRNLD SQHDR

HSOGENIES & ISOMETRIES

ITPHF0JFT & JTPNFUSJFT

JUQIGPKGU & KUQOGVTKGU

KVRJHQLHV & LVRPHWULHV

L

M

N

GQMECLGCO

HRNFDMHDR

ISOGENIES

JTPHF0JFT

KUQIGPKGUG

LVRJHQLHV

&

&

&

&

&

&

GQMKCRPGCO

HRNLD SQHDR

ISOMETRIES

JTPNFUSJFT

KUQ0GVTKGU

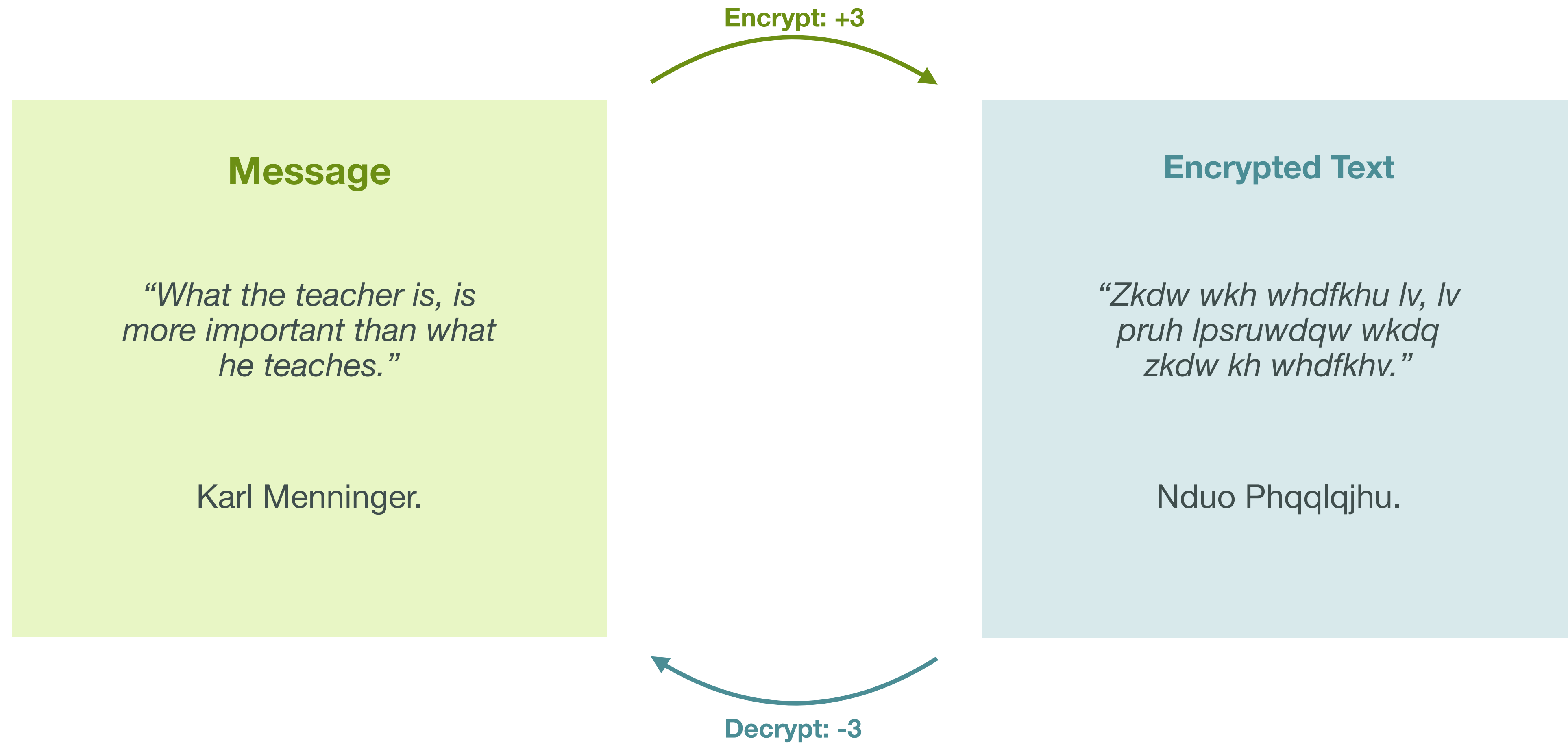
LVRPHWULHV

ISOGENIES & ISOMETRIES

ISOGENIES & ISOMETRIES

Krijn Reijnders - 10.30 - May 12, 2025

Our First Encryption!



(Diffie and Hellman, 1976)

MESSAGE: Innovation [...] has come primarily from the amateurs

KEYWORD: crypto
(repeats)

(Diffie and Hellman, 1976)

MESSAGE: Innovation [...] has come primarily from the amateurs

KEYWORD: **crypto**cryp [...] toc rypt ocryptocr ypto cry ptocrypt
(repeats)

(Diffie and Hellman, 1976)

MESSAGE: Innovation [...] has come primarily from the amateurs

09

KEYWORD: **crypto**cryp [...] toc rypt ocryptocr ypto cry ptocrypt
(repeats)

03

12

L

(Diffie and Hellman, 1976)

MESSAGE: Innovation [...] has come primarily from the amateurs
09 14 14 15 22 01 20 09 15 14 [...] 08 01 19 03 15 13 05 16 18 09 13 01 18 09 12 25 06 18 15 13 20 08 05 01 13 01 20 05 21 18 19

KEYWORD: **cryptocryp** [...] toc rypt ocryptocr ypto cry ptocrypt
(repeats)
03 18 25 16 20 15 03 18 25 16 [...] 20 15 03 18 25 16 20 15 03 18 25 16 20 15 03 18 25 16 20 15 03 18 25 16 20

12 06 13 05 16 16 23 01 14 04 [...] 02 06 22 21 14 03 25 05 21 01 12 17 12 24 15 17 05 08 09 02 23 26 04 17 07 16 23 23 20 08 13

ENCRYPTION: Lfmeppwand [...] bpv uncy eualqlxoq ehíb wzd qgpwwthm

Vigenère Encryption!

Encrypt with keyword



Message

*Innovation, particularly in the design of
new types of cryptographic systems,
has come primarily from the amateurs.*

Diffie and Hellman, 1976.

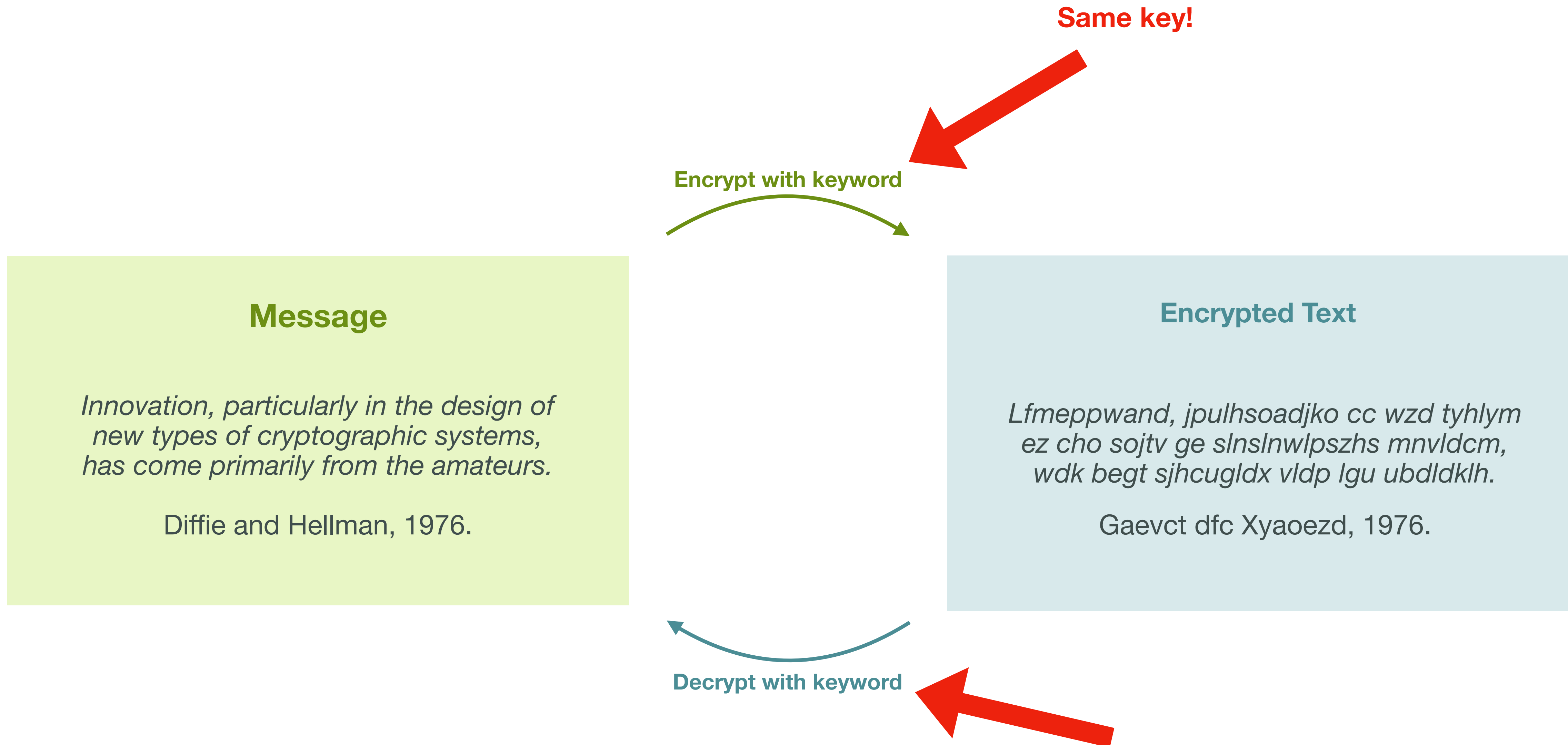
Encrypted Text

*Lfmeppwand, jpulhsoadjko cc wzd tyhlym
ez cho sojtv ge slnslnwlpszhs mnvldcm,
wdk begt sjhcugldx vldp lgu ubdldklh.*

Gaevct dfc Xyaoezd, 1976.

Decrypt with keyword





Same key!

Encrypt with keyword

Message

SAME-KEY CRYPTOGRAPHY

(symmetric cryptography)

Encrypted Text

Decrypt with keyword



Encrypt with keyword

Same key!

Message

Encrypted Text

SAME-KEY CRYPTOGRAPHY

(symmetric cryptography)

Decrypt with keyword

*Innovation, particularly in the design of
new types of cryptographic systems,
has come primarily from the amateur.*

Diffie and Hellman, 1976.

*Lfmeppwand, jpulhsoadjko, cc wzd tyhlym
je slnslnwlpshs mnvlcdm,
vldp lgu ubdldklh.*

Gaevct dfc Xyaoezd, 1976.



Encrypt with my
public lock



Message

*Innovation, particularly in the design of
new types of cryptographic systems,
has come primarily from the amateurs.*

Diffie and Hellman, 1976.

Encrypted Text

*Lfmeppwand, jpulhsoadjko cc wzd tyhlym
ez cho sojtv ge slnslnwlpszhs mnvldcm,
wdk begt sjhcugldx vldp lgu ubdldklh.*

Gaevct dfc Xyaoezd, 1976.

Decrypt with my own
secret key





Encrypt with my
public lock

Message

LOCK-AND-KEY CRYPTOGRAPHY

Encrypted Text

*Innovation, particularly in the design of
new types of cryptographic systems,
has come primarily from the*

Diffie and Hellman, 1976.

*(asymmetric cryptography,
public key cryptography)*

*Lfmenppwond jpuhlsoadjko cc wzd tyhlym
ge slnslnwlpszhs mnvlbcm,
wot bgt jhcugldx vldp lgu ubdldklh.*

Gaevct dfc Xyaoezd, 1976.

Decrypt with my own
secret key





Encrypt with my
public lock



Message

LOCK-AND-KEY CRYPTOGRAPHY

Encrypted Text

*Innovation, particularly in the design of
new types of cryptographic systems,
has come primarily from the military.*

Diffie and Hellman, 1976.

*(asymmetric cryptography,
public key cryptography)*

*L fmenppwond jpuhlsoadjko cc wzd tyhlym
wzd tyhlym, ge slnslnwlpshs mnvldcm,
wzd tyhlym jhcugldx vldp lgu ubdldklh.*

Gaevct dfc Xyaoezd, 1976.

Decrypt with my own
secret key





SAME-KEY CRYPTOGRAPHY

(symmetric cryptography)



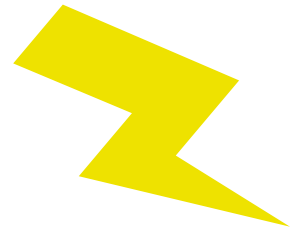
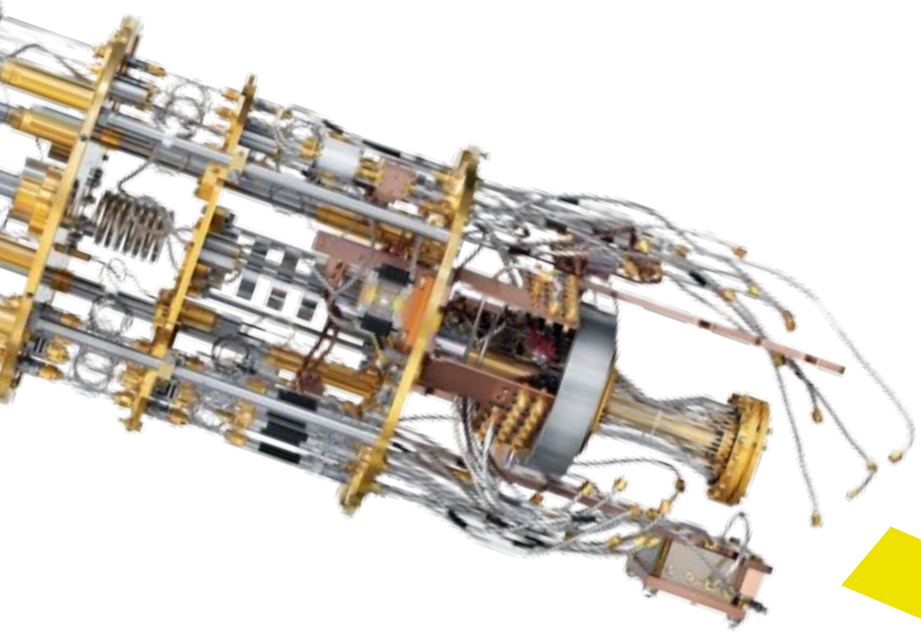
LOCK-AND-KEY CRYPTOGRAPHY

*(asymmetric cryptography,
public key cryptography)*



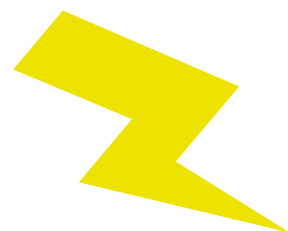
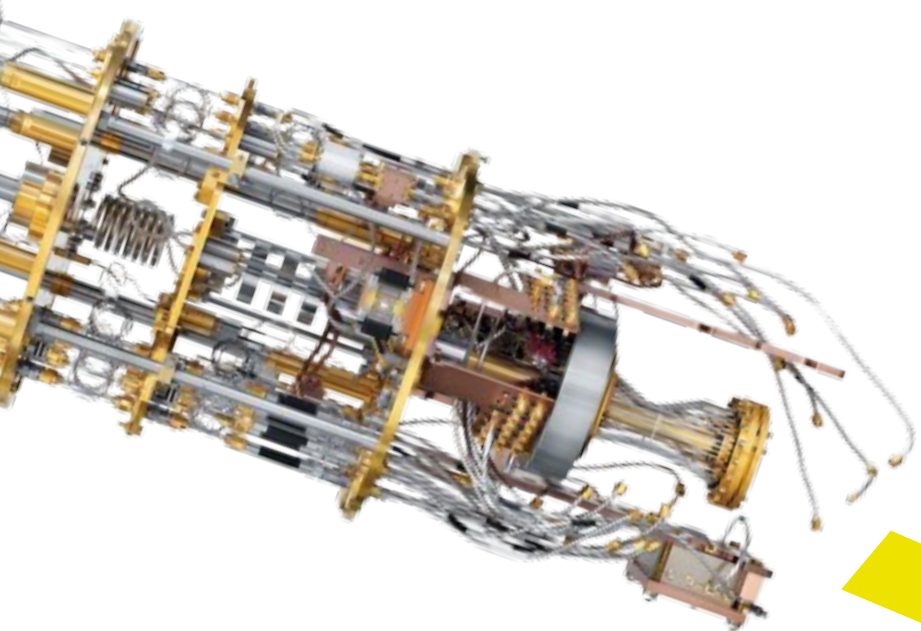
SAME-KEY CRYPTOGRAPHY

(symmetric cryptography)



LOCK-AND-KEY CRYPTOGRAPHY

*(asymmetric cryptography,
public key cryptography)*



SAME-KEY CRYPTOGRAPHY

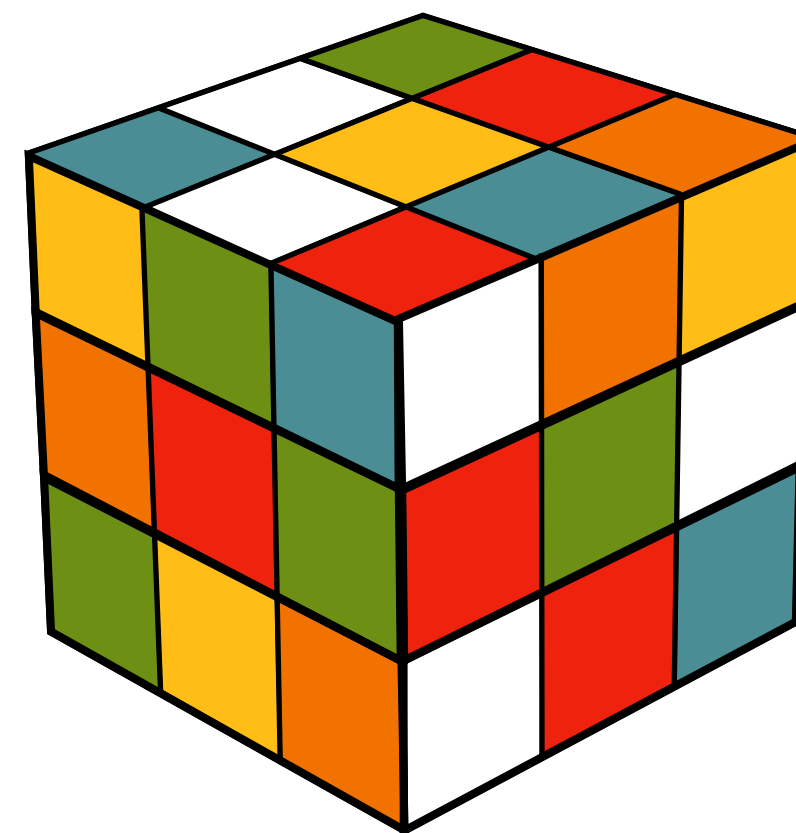
(symmetric cryptography)

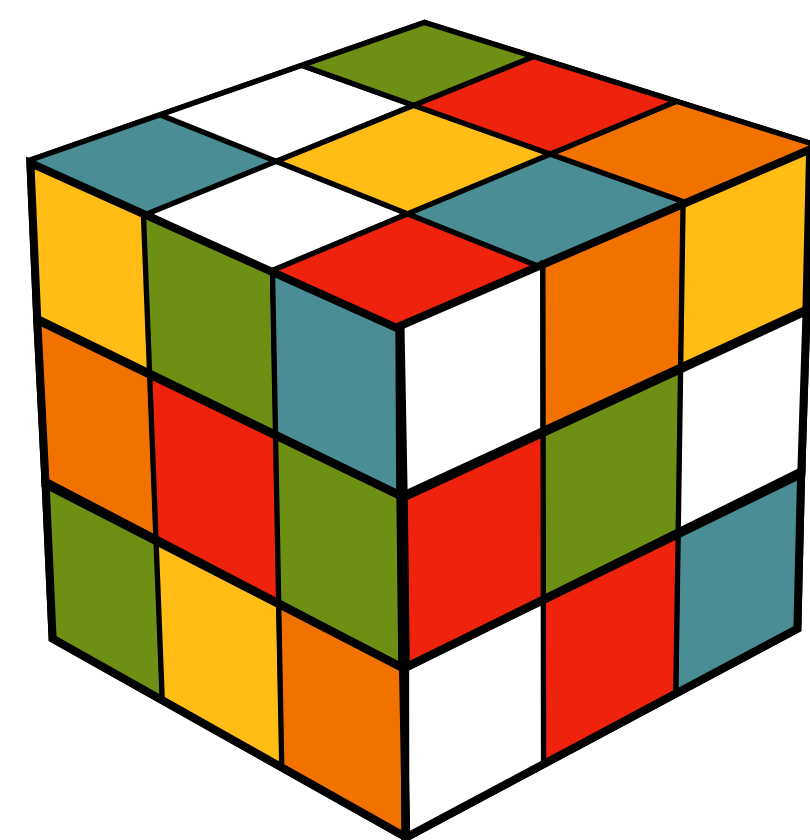


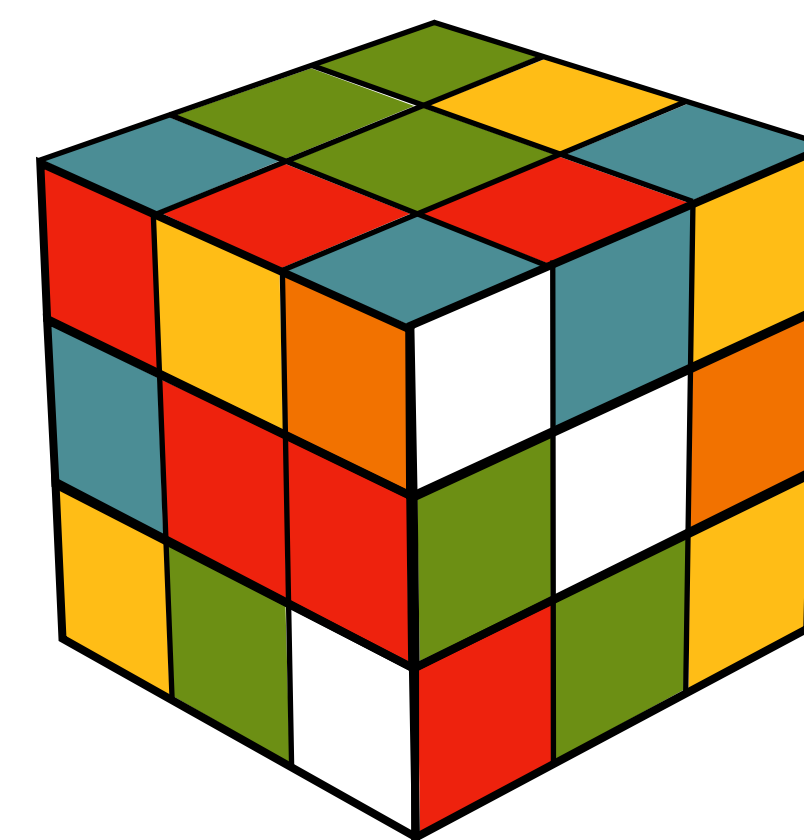
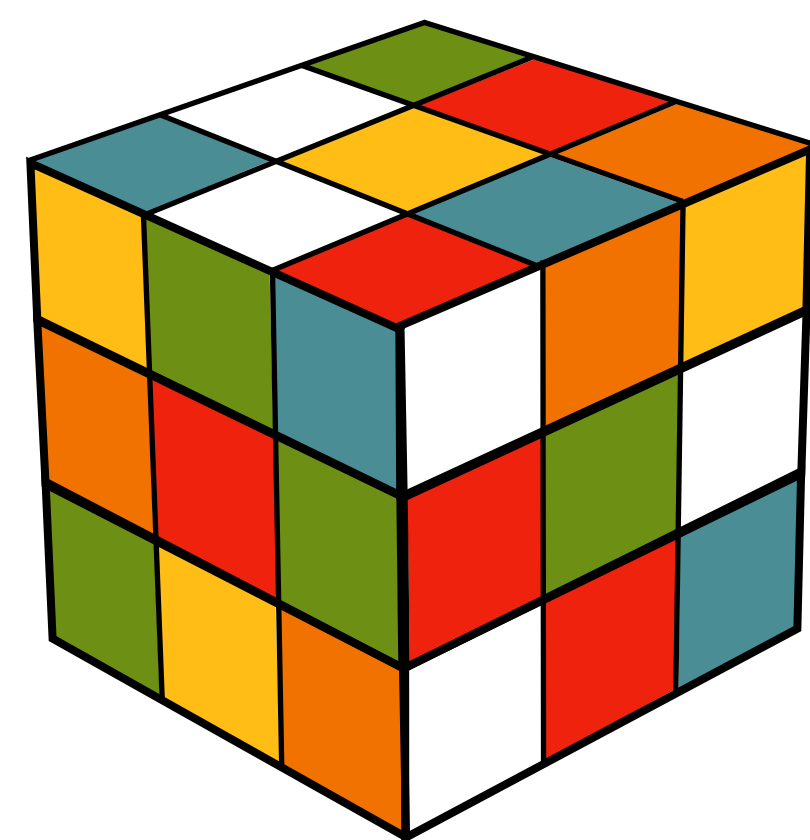
POST-QUANTUM CRYPTOGRAPHY

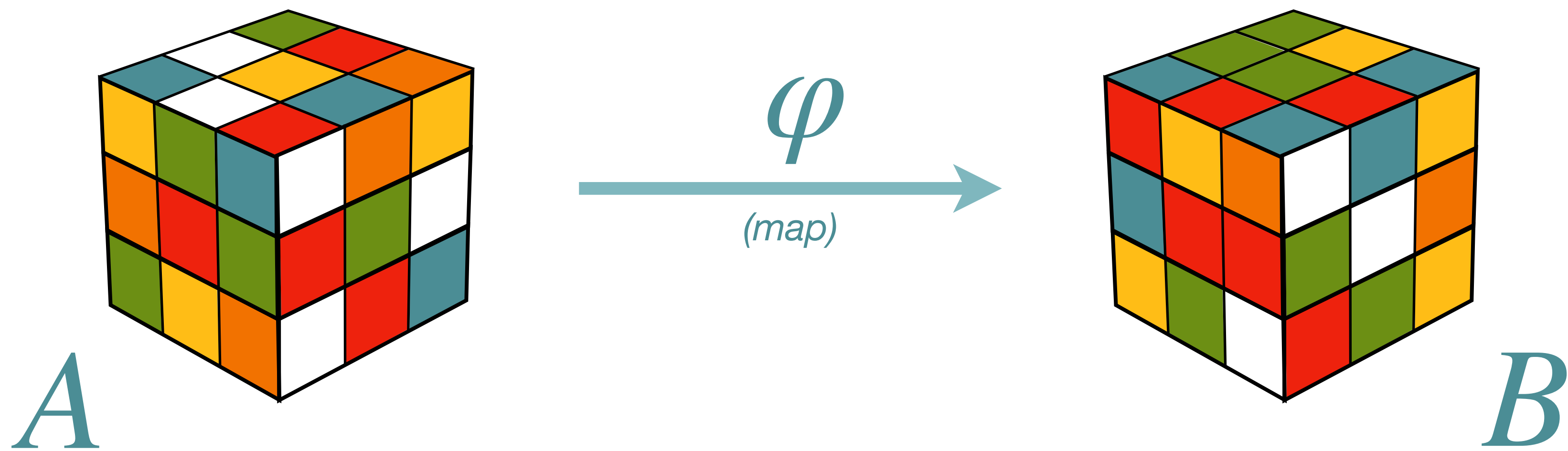
ISOGENIES & ISOMETRIES

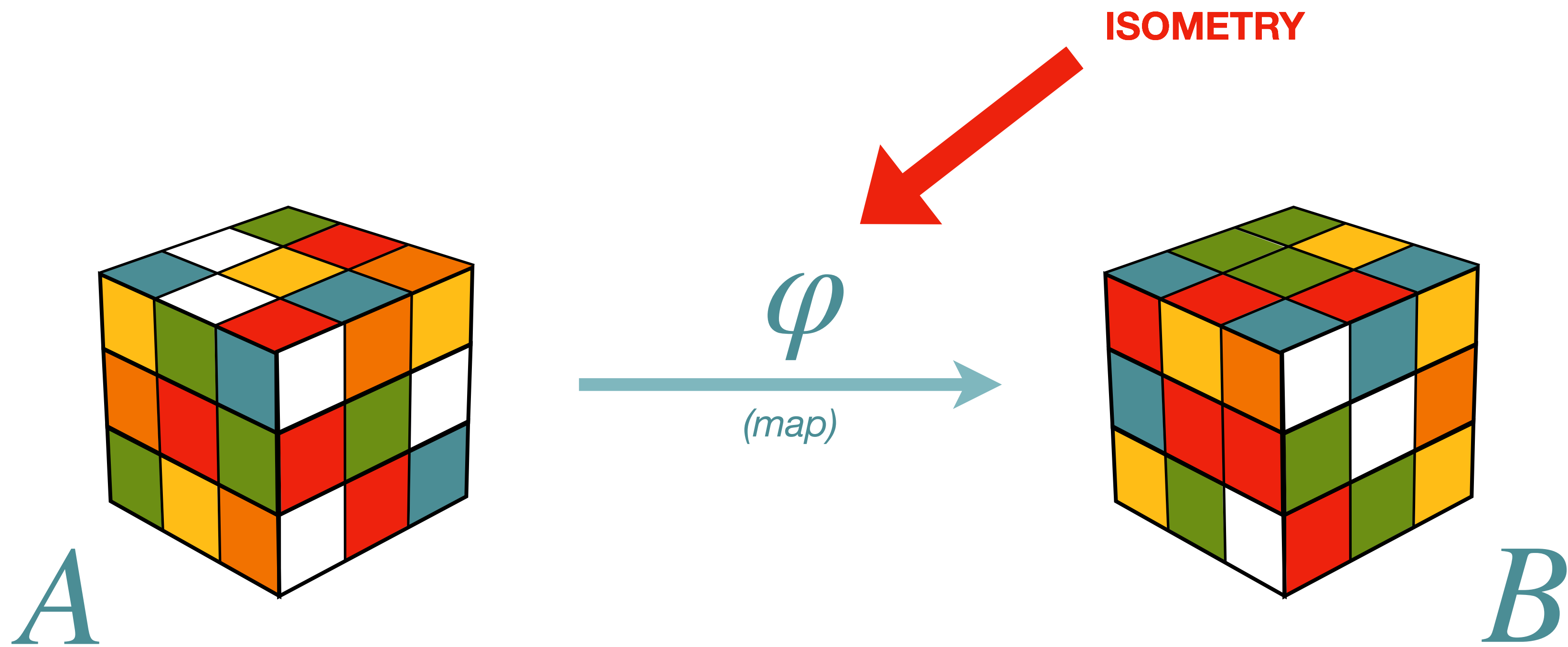
Krijn Reijnders - 10.30 - May 12, 2025

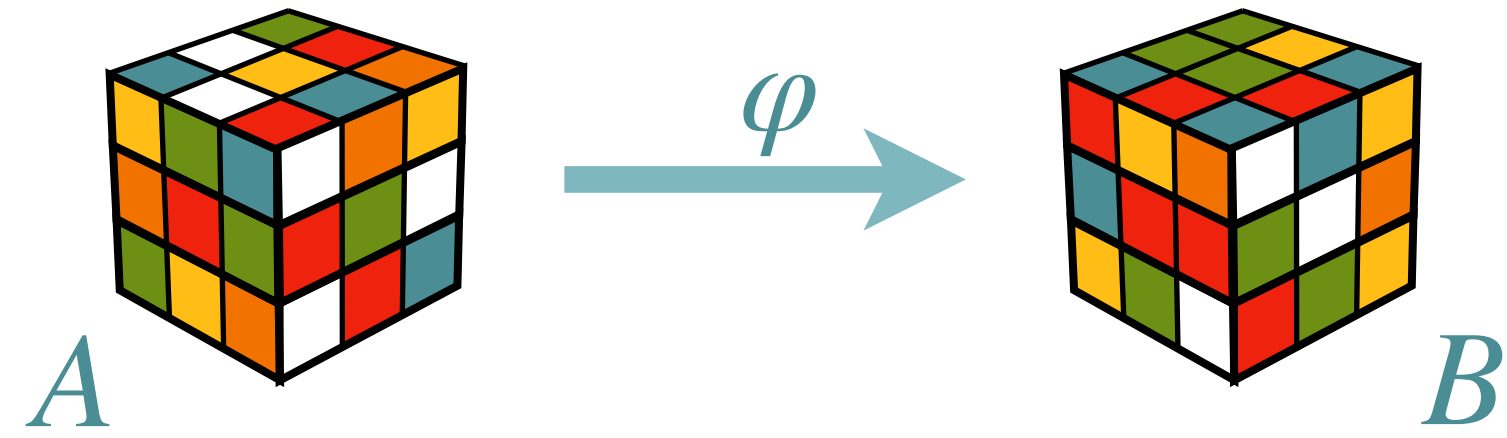










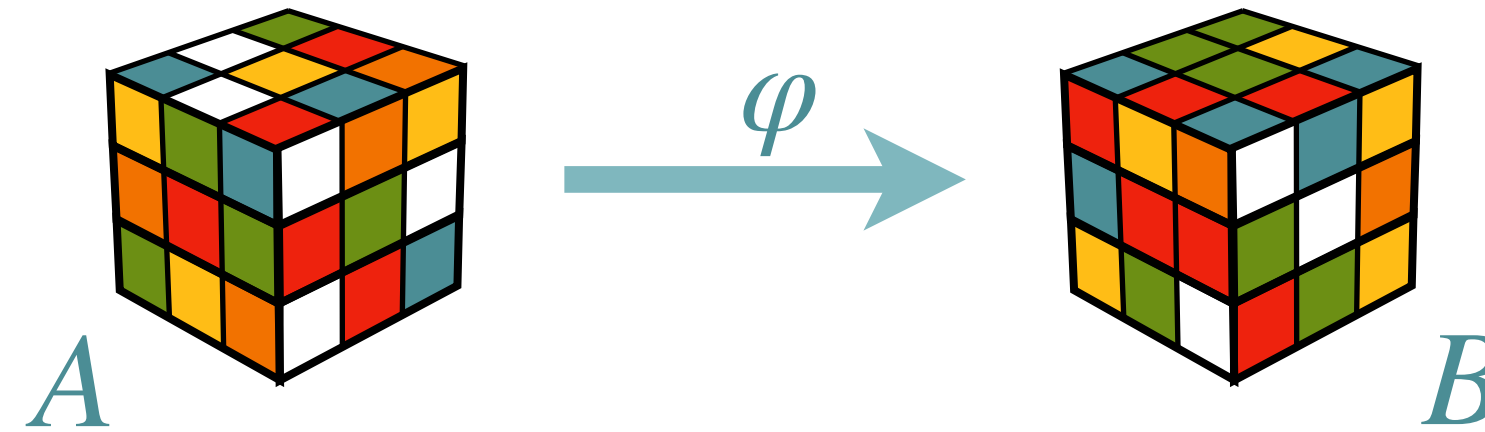


analysis

Understanding
these maps

design

Build cryptography
from these maps



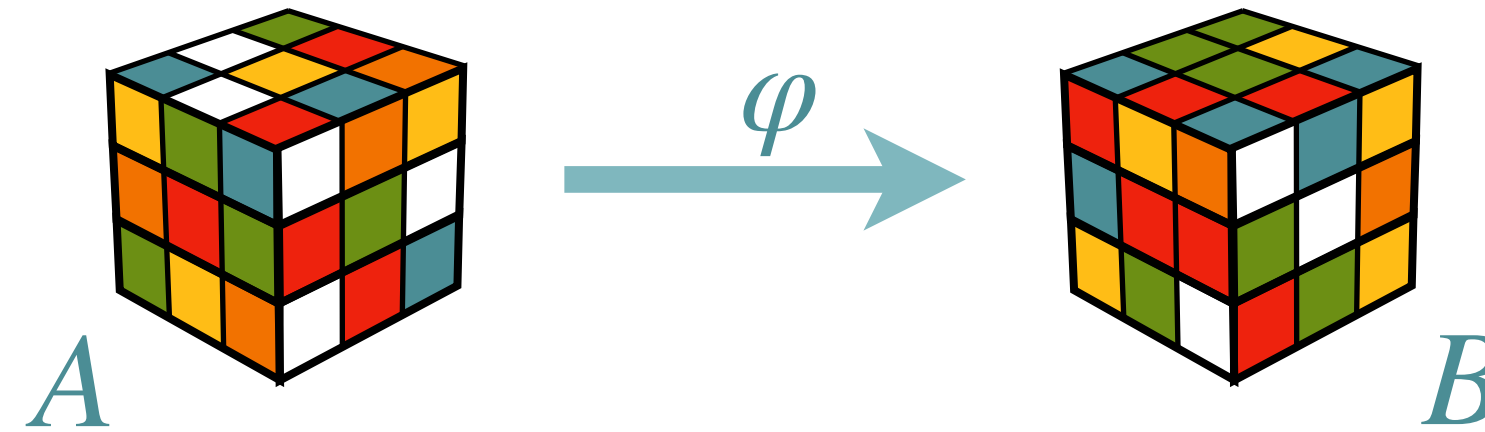
analysis

Understanding
these maps

- if we know the objects A and B ,
how **hard** is it to find the map φ ?
- if we have a **quantum computer**,
is it easier to find the map φ ?
- when we compute φ in practice,
do we **leak information** on φ ?

design

Build cryptography
from these maps



analysis

Understanding
these maps

- if we know the objects A and B , how **hard** is it to find the map φ ?
- if we have a **quantum computer**, is it easier to find the map φ ?
- when we compute φ in practice, do we **leak information** on φ ?

design

Build cryptography
from these maps

- how **versatile** is cryptography using these type of maps φ ?
- how **efficient** is cryptography using these type of maps φ ?
- can we use **smarter maths** to compute φ more efficiently?

	ISOGENIES	ISOMETRIES
analysis		
design		

ISOGENIES

ISOMETRIES

Chapter 4

if you **listen carefully**
to your chip, you can
learn secret isogenies

analysis

design

ISOGENIES

ISOMETRIES

analysis

Chapter 4

if you **listen carefully**
to your chip, you can
learn secret isogenies

Chapter 5

if you **shoot lasers**
at your chip, you can
learn secret isogenies

design

ISOGENIES

ISOMETRIES

analysis

Chapter 4

if you **listen carefully**
to your chip, you can
learn secret isogenies

Chapter 5

if you **shoot lasers**
at your chip, you can
learn secret isogenies

design

Chapter 6 & 8

using **smarter maths**
makes certain isogenies
faster and safer

ISOGENIES

ISOMETRIES

analysis

Chapter 4

if you **listen carefully**
to your chip, you can
learn secret isogenies

Chapter 5

if you **shoot lasers**
at your chip, you can
learn secret isogenies

design

Chapter 6 & 8

using **smarter maths**
makes certain isogenies
faster and safer

Chapter 7

if you make everything
super safe for isogenies,
it all becomes very slow

ISOGENIES

ISOMETRIES

analysis

Chapter 4

if you **listen carefully**
to your chip, you can
learn secret isogenies

Chapter 5

if you **shoot lasers**
at your chip, you can
learn secret isogenies

design

Chapter 6 & 8

using **smarter maths**
makes certain isogenies
faster and safer

Chapter 7

if you make everything
super safe for isogenies,
it all becomes very slow

Chapter 9 & 10

we can make certain
isogenies **much faster**,
if we make others slow

ISOGENIES

ISOMETRIES

analysis

Chapter 4

if you **listen carefully**
to your chip, you can
learn secret isogenies

Chapter 5

if you **shoot lasers**
at your chip, you can
learn secret isogenies

design

Chapter 6 & 8

using **smarter maths**
makes certain isogenies
faster and safer

Chapter 7

if you make everything
super safe for isogenies,
it all becomes very slow

Chapter 9 & 10

we can make certain
isogenies **much faster**,
if we make others slow

Chapter 11

using more complex maths
makes some isogenies
very cool but slow

ISOGENIES

ISOMETRIES

analysis

Chapter 4

if you **listen carefully**
to your chip, you can
learn secret isogenies

Chapter 5

if you **shoot lasers**
at your chip, you can
learn secret isogenies

Chapter 12

our **new algorithm** finds
secret isometries faster,
but its still very hard

design

Chapter 6 & 8

using **smarter maths**
makes certain isogenies
faster and safer

Chapter 7

if you make everything
super safe for isogenies,
it all becomes very slow

Chapter 9 & 10

we can make certain
isogenies **much faster**,
if we make others slow

Chapter 11

using more complex maths
makes some isogenies
very cool but slow

ISOGENIES

ISOMETRIES

analysis

Chapter 4

if you **listen carefully**
to your chip, you can
learn secret isogenies

Chapter 5

if you **shoot lasers**
at your chip, you can
learn secret isogenies

Chapter 12

our **new algorithm** finds
secret isometries faster,
but its still very hard

design

Chapter 6 & 8

using **smarter maths**
makes certain isogenies
faster and safer

Chapter 7

if you make everything
super safe for isogenies,
it all becomes very slow

Chapter 13

we make **digital signatures**
from isometries, but...
they're slow and big

Chapter 9 & 10

we can make certain
isogenies **much faster**,
if we make others slow

Chapter 11

using more complex maths
makes some isogenies
very cool but slow

ISOGENIES

ISOMETRIES

analysis

Chapter 4

if you **listen carefully**
to your chip, you can
learn secret isogenies

Chapter 5

if you **shoot lasers**
at your chip, you can
learn secret isogenies

Chapter 12

our **new algorithm** finds
secret isometries faster,
but its still very hard

design

Chapter 6 & 8

using **smarter maths**
makes certain isogenies
faster and safer

Chapter 7

if you make everything
super safe for isogenies,
it all becomes very slow

Chapter 13

we make **digital signatures**
from isometries, but...
they're slow and big

Chapter 9 & 10

we can make certain
isogenies **much faster**,
if we make others slow

Chapter 11

using more complex maths
makes some isogenies
very cool but slow

Chapter 14

you can use maths to
make these signatures
smaller and faster

ISOGENIES

ISOMETRIES

analysis

Chapter 4

if you **listen carefully**
to your chip, you can
learn secret isogenies

Chapter 5

if you **shoot lasers**
at your chip, you can
learn secret isogenies

Chapter 12

our **new algorithm** finds
secret isometries faster,
but its still very hard

design

Chapter 6 & 8

using **smarter maths**
makes certain isogenies
faster and safer

Chapter 7

if you make everything
super safe for isogenies,
it all becomes very slow

Chapter 13

we make **digital signatures**
from isometries, but...
they're slow and big

Chapter 9 & 10

we can make certain
isogenies **much faster**,
if we make others slow

Chapter 11

using more complex maths
makes some isogenies
very cool but slow

Chapter 14

you can use maths to
make these signatures
smaller and faster

1

Certain cryptography made from isogenies (CSIDH) is now faster and more secure, but **not yet ready** for the real world.

ISO $\rightarrow$ GEN



METR $\rightarrow$ IES



1

Certain cryptography made from isogenies (CSIDH) is now faster and more secure, but **not yet ready** for the real world.

2

Other cryptography made from isogenies (SQIsign) is now faster and more secure, and looks **pretty promising** for the future!

1

Certain cryptography made from isogenies (CSIDH) is now faster and more secure, but **not yet ready** for the real world.

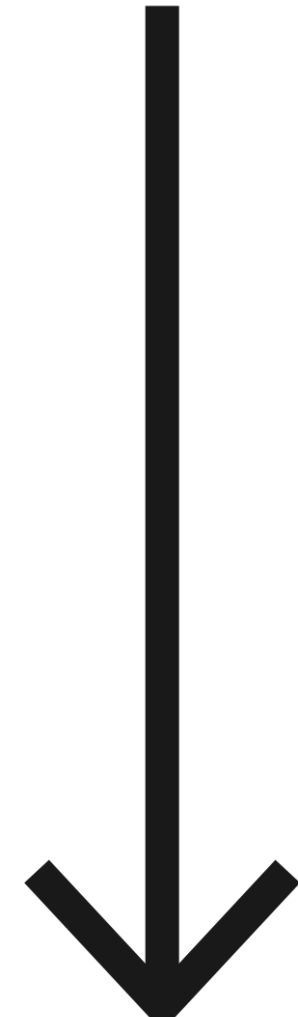
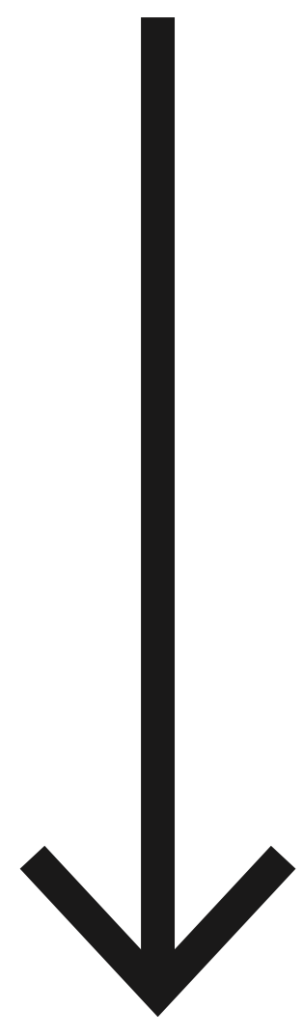
2

Other cryptography made from isogenies (SQIsign) is now faster and more secure, and looks **pretty promising** for the future!

3

Our cryptography made from isometries (MCE) is a nice try, but has **major issues**... We should be more bold with isometries!

ISO → *GEN*



METR → **IES**